## Finstall First School



How we teach calculations:

## Calculation Policy for Mathematics

## January 2019

We care, we share, we learn and achieve

The following calculation policy has been devised to meet the requirements of the National Curriculum 2014 for the teaching and learning of mathematics. It shows the progression of learning of calculations across the school. Please note that early learning in number and calculation, taught in Reception, follows the Early Years Foundation Stage.

## Age related expectations

The calculation policy is organised according to typical age-related expectations, as set out in the National Curriculum 2014. However it is vital that pupils are taught according to the level of ability and understanding that they are currently working at. They should only progress onto the next stage when they are ready and they feel secure enough to move on.

## Providing a context for calculation:

It is important that any type of calculation is given a real life context. A relevant problem solving approach helps to build children's understanding of the purpose of calculation and helps them to recognise when to use certain operations and methods when faced with problems. This is a priority within calculation lessons at Finstall First School.

## Choosing a calculation method

Children need to be taught and encouraged to use the following process when deciding which approach they will take in order to solve a calculation. This will help to ensure that they select the most appropriate method for the numbers involved.

| Can I do it in my head using a mental strategy? |
| :---: |
| Could I use some jottings to help me? |
| Should I use a written method to work it out? |

## Reception Add with numbers up to 20

Children become increasing familiar with the number up to 20. They use practical and pictorial methods to add by combining two sets of objects and counting on in ones.
The children will also be introduced to informal jottings and the use of the addition $(+)$ and equals ( $=$ ) symbols.


$$
5+1=6
$$



## Children should:

- Have access to a wide range of counting equipment: unfix cubes, numicon, counting beads etc.
- Be shown and use simple calculations using pictorial representations.
- Be shown numbers in different contexts.
- Be introduced to the addition (+) and equals ( $=$ ) signs within simple number

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line.
Key skills for addition in Reception:

- Read and write numbers from 0 to 20 in numerals and words.
- Given a number, say one more or one less.
- Count to and over 20, forward and back.
- Solve simple practical and pictorial problems that involve addition.
- Combine two groups of objects to find a total.
- Add by counting on from a given number (using both practical and pictorial methods).


## Year 1 Add with numbers up to 20

Use numbered number lines to add, by counting on in ones. Encourage children to start with the larger number and count on.
$6+3=9$


## Children should:

- Have access to a wide range of counting equipment: everyday objects, number tracks and number lines.
- Be shown numbers in different contexts.
- Read and write the addition (+) and equals (=) signs within number sentences.
- Interpret addition number sentences and solve missing number problems, using concrete objects and number line addition to solve them:

$$
8+3=\square \quad 15+4=\square \quad 5+3+1=\square \quad \square+\square=6
$$

This builds on from prior learning of adding by combining two sets of objects into one group ( 5 cubes and 3 cubes) in Early Years.

Bead strings or bead bars can be used to illustrate addition including bridging through ten by counting on 2 then counting on 3 .

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line.
Key skills for addition at Y 1 :

- Read and write numbers to 100 in numerals, incl. 1-20 in words
- Recall bonds to 10 and 20
- Addition facts within 20
- Count to and across 100
- Count in multiples of $1,2,5$ and 10
- Solve simple 1-step problems involving addition, using objects, number lines and pictorial representations.


## Year 2 Add with 2-digit numbers. Developing mental fluency with addition and

place value involving 2-digit numbers, then establishing more formal methods.

Add 2-digit numbers and tens:
$27+30$
$+10+10+10$

$\begin{array}{llll}27 & 37 & 47 & 57\end{array}$

Add 2-digit numbers and units:
Use blank number lines, concrete equipment, hundred squares etc. to build confidence and fluency in mental addition skills
$16+7$


Add pairs of 2-digit numbers, moving to the partitioned column method when secure (adding tens and units):


STEP 1: Only provide examples that do NOT cross the tens boundary until they are secure with the method itself.

STEP 2: Once children can add a multiple of ten to a 2-digit number mentally (e.9. 80+11), they are ready for adding pairs of 2-digit numbers that DO cross the tens boundary (e.g. $58+43$ ).


STEP 3: Children who are confident and accurate with this stage should move onto the expanded addition methods with 2 and 3 -digit numbers (see $Y 3$ ).

To support understanding, pupils may physically make and carry out the calculation with apparatus, then compare their practical version to the written form, to help them to build an understanding of it.

## Year 2 Addition (continued)

Key vocabulary: : add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary.

## Key skills for addition at Y2:

- Add a 2-digit number and ones (e.g. 27 + 6).
- Add a 2 -digit number and tens (e.g. $23+40$ ).
- Add pairs of 2 -digit numbers (e.g. $35+47$ ).
- Add three single-digit numbers (e.g. $5+9+7$ ).
- Show that adding can be done in any order (the commutative law).
- Recall bonds to 20 and bonds of tens to $100(30+70$ etc. $)$.
- Count in steps of 2,3 and 5 and count in tens from any number.
- Understand the place value of 2-digit numbers (tens and ones).
- Compare and order numbers to 100 using < > and = signs.
- Read and write numbers to at least 100 in numerals and words.
- Solve addition problems in a range of contexts (numbers, quantities and measures) using concrete objects, pictorial representations and by applying mental and written methods.
- To use the symbols + and =.


## Year 3 Add numbers with up to 3-digits.

Introduce the expanded column addition method:

## In order to carry out this method of addition:

- Children need to recognise the value of the hundreds, tens and units without recording the partitioning.
- Pupils need to be able to add in columns.

Move to the compact column addition method, with 'carrying':


## Year 3 Addition (continued)

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact.

Key skills for addition at Y3:

- Read and write numbers to 1000 in numerals and words.
- Add 2-digit numbers mentally, incl. those additions exceeding 100.
- Add a three-digit number and ones mentally (175 + 8)
- Add a three-digit number and tens mentally (249 + 50)
- Add a three-digit number and hundreds mentally $(381+400)$
- Estimate answers to calculations, using inverse to check answers.
- Solve problems, including missing number problems, using number facts, place value, and more complex addition.
- Recognise place value of each digit in 3-digit numbers (hundreds, tens, units.)
- Continue to practise a wide range of mental addition strategies, i.e. number bonds, adding the nearest multiple of $10,100,1000$ and adjusting, using near doubles, partitioning and recombining.


## Year 4 Add numbers with up to 4 digits

Move from expanded addition to the compact column method, adding units first, and 'carrying' numbers underneath the calculation. Also include money and measures contexts.


Use and apply this method to money and measurement values.

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, vertical, 'carry', expanded, compact, thousands, hundreds, digits, inverse.

## Key skills for addition at Y4:

- Select most appropriate method: mental, jottings or written and explain why.
- Recognise the place value of each digit in a four-digit number.
- Round any number to the nearest 10,100 or 1000.
- Estimate and use inverse operations to check answers.
- Solve 2-step problems in context, deciding which operations and methods to use and why.
- Find 1000 more or less than a given number.
- Continue to practise a wide range of mental addition strategies, i.e. number bonds, add the nearest multiple of $10,100,1000$ and adjust, use near doubles, partitioning and recombining.
- Add numbers with up to 4 digits using the formal written method of column addition
- Solve 2-step problems in contexts, deciding which operations and methods.


## Year 5 Add numbers with more than 4 digits including money,

 measures and decimals (with different numbers of decimal places).

The decimal point should be aligned in the same way as the other place value columns, and must be in the same column in the answer


Numbers should exceed 4 digits.


## Children should:

Understand the place value of tenths and hundredths and use this to align numbers with different numbers of decimal places.

## Year 5 Addition (continued)

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, "carry", expanded, compact, vertical, thousands, hundreds, digits, inverse, decimal places, decimal point, tenths, hundredths, thousandths.

## Key skills for addition at Y 5 :

- Add numbers mentally with increasingly large numbers, using and practising a range of mental strategies i.e. add the nearest multiple of $10,100,1000$ and adjust; use near doubles, inverse, partitioning and re-combining; using number bonds.
- Use rounding to check answers and accuracy.
- Solve multi-step problems in contexts, deciding which operations and methods to use and why.
- Read, write, order and compare numbers to at least 1 million and determine the value of each digit.
- Round any number up to 1000000 to the nearest $10,100,1000,10000$ and 100000.
- Add numbers with more than 4 digits using formal written method of columnar addition.


## Year 6 Add several numbers of increasing complexity



Adding several numbers with more than 4 digits

Key vocabulary: add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, plus, addition, column, tens boundary, hundreds boundary, increase, "carry", expanded, compact, vertical, thousands, hundreds, digits, inverse, decimal places, decimal point, tenths, hundredths, thousandths

## Key skills for addition at Y6:

- Perform mental calculations, including with mixed operations and large numbers, using and practising a range of mental strategies.
- Solve multi-step problems in context, deciding which operations and methods to use and why.
- Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy.
- Read, write, order and compare numbers up to 10 million and determine the value of each digit.
- Round any whole number to a required degree of accuracy.
- Pupils understand how to add mentally with larger numbers and calculations of increasing complexity.


## Reception Subtract from numbers up to 20.

Children develop an understanding of subtraction practically, showing subtraction on bead strings and using cubes, other objects and pictures. They carry out simple subtractions within familiar contexts. The children will also be introduced to informal jottings and the subtraction (-) and equals (=) signs.

- ○○○
5-1=4



## Children should:

- Have access to a wide range of practical equipment: unfix cubes, numicon, counting beads etc.
- Be shown and use simple calculations using pictorial representations.
- Be shown numbers and simple subtractions in different contexts.
- Be introduced to the subtraction (-) and equals (=) signs within simple number sentences.

Key vocabulary: take away, less, how many fewer/less than, most, least, how many left?
Key skills for subtraction in Reception:

- Read and write numbers from 0 to 20 in numerals and words.
- Given a number, say one more or one less.
- Count to and over 20, forward and back.
- Subtract practically with one-digit and two-digit numbers to 20.
- Solve simple practical and pictorial problems that involve subtraction.
- Use the subtraction (-) and equals (=) symbols.


## Year 1 subtract from numbers up to 20.

Children consolidate understanding of subtraction practically, showing subtraction on bead strings, using cubes etc. and in familiar contexts. They are introduced to more formal recording methods using number lines (see below) and learn to read, write and interpret number sentences with - and = signs.

Subtract by taking away:


Count back in ones on a numbered number line to take away, with numbers up to 20

$$
7-4=3
$$

Model subtraction using hundred squares and numbered number lines/tracks and practically.

Finding the difference:

'I am 2 years older than my sister'

This will be introduced practically with the language 'find the distance between' and 'how many more?' in a range of familiar contexts.

## Mental subtraction:

Children should start recalling subtraction facts up to and within 10 and 20.

## Year 1 Subtraction (continued)

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, difference/how many between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is_?

## Key skills for subtraction at Y 1 :

- Given a number, say one more or one less.
- Count to and over 100, forward and back, from any number.
- Represent and use subtraction facts to 20 and within 20.
- Subtract with one-digit and two-digit numbers to 20, including zero.
- Solve one-step problems that involve addition and subtraction, using concrete objects (i.e. bead string, objects, cubes) and pictures.
- To use subtraction to solve missing number problems.
- Read and write numbers from 0 to 20 in numerals and words.


## Year 2 Subtract with 2-digit numbers.

Subtract on a number line by counting back, aiming to develop mental subtraction skills.
This strategy will be used for:

- 2-digit numbers subtract 1-digit numbers (by taking away/counting back) e.g. 38-7
- 2-digit numbers subtract tens (by taking away/counting back) e.g. 48-30
- Subtracting pairs of 2-digit numbers (see below:)


Mental strategy - subtract numbers close together by counting on:
$42-38=4$


Many mental strategies are taught. Children are taught to recognise that when numbers are close together, it is more efficient to count on the difference. They need to be clear about the relationship between addition and subtraction.

## Year 2 Subtraction (continued)

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, difference/how many between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units.

## Key skills for subtraction at y2:

- Recognise the place value of each digit in a two-digit number and how to use place value to solve subtractions.
- Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100.
- Subtract using concrete objects, pictorial representations, number lines and 100 squares.
- Subtract mentally, including: a two-digit number and units, a two-digit number and tens, and two two-digit numbers.
- Show that subtraction of one number from another cannot be done in any order (is not commutative).
- Recognise and use the inverse relationship between addition and subtraction, using this to check calculations and solve missing number problems.
- Solve simple subtraction problems in a range of contexts (measures, money etc.) using concrete objects, pictorial representation and also by apply increasing knowledge of mental and written methods.
- Read and write numbers to at least 100 in numerals and in words.
- To use the symbols - and =.


## Year 3 Subtracting with 2 and 3-digit numbers.

Introduce partitioned column subtraction method.

STEP 1: introduce this method with examples where no exchanging is required.

$$
\begin{aligned}
& 89-35=54 \\
& 80+9 \\
& \frac{-30+5}{50+4}
\end{aligned}
$$

STEP 2: introduce 'exchanging"through subtraction.
$72-47=25$

$$
70+2 \text { or } 60+12
$$

$$
-40+7
$$

$$
20+5=\underline{25}
$$

When learning to 'exchange', explore 'partitioning in different ways' so that pupils understand that when you exchange, the

VALUE is the same i.e. $72=70+2=60+12=50+22$ etc.
Emphasise that the value hasn't changed, we have just partitioned it in a different way.

STEP 3: Once pupils are secure with the understanding of "exchanging", they can use the partitioned column method to subtract any 2 and 3-digit numbers.

$$
\begin{array}{r}
238-146=92 \\
-2000+30+8 \\
-\frac{100+40+6}{10+90+2} \\
\hline
\end{array}
$$



Counting on as a mental strategy for subtraction:

Continue to reinforce counting on as a strategy for close-together numbers (e.g. 121-118), and also for numbers that are "nearly" multiples of $10,100,1000$ or $£ s$, which make it easier to count on (e.g. 102-89, 131-79, or calculating change from $£ 1$ etc.).

- Start at the smaller number and count on in tens first, then count on in units to find the rest of the difference.



## Year 3 Subtraction (continued)

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, difference/how many between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units, exchange, decrease, hundreds, value, digit.

## Key skills for subtraction at Y 3 :

- Subtract mentally a: 3-digit number and units, 3-digit number and tens, 3-digit number and hundreds.
- Estimate answers and use inverse operations to check.
- Solve problems, including missing number problems.
- Find 10 or 100 less than a given number.
- Recognise the place value of each digit in a 3-digit number and use this knowledge to solve subtraction problems.
- Counting up differences as a mental strategy when numbers are close together or near multiples of 10 .
- Read and write numbers up to 1000 in numerals and words.
- Practise mental subtraction strategies, such as subtracting near multiples of 10 and adjusting (e.g. subtracting 19 or 21), and select the most appropriate methods to subtract, explaining why.


## Year 4 Subtract with up to 4-digit numbers.

Partitioned column subtraction with "exchanging" (decomposition):


Compact column subtraction
To introduce the compact method, ask children to perform a subtraction calculation with the familiar partitioned column subtraction then display the compact version for the calculation they have done. Ask pupils to consider how it relates to the method they know, what is similar and what is different, to develop an understanding of it.


## Mental strategies:

A variety of mental strategies must be taught and practised, including counting on to find the difference where numbers are closer together, or where it is easier to count on.

## Year 4 Subtraction (continued)

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, difference/how many between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit, inverse.

## Key skills for subtraction at Y4:

- Subtract by counting on where numbers are close together or they are near to multiples of 10 , 100 etc.
- Children select the most appropriate and efficient methods for given subtraction calculations.
- Estimate and use inverse operations to check answers.
- Solve subtraction 2-step problems, choosing which operations and methods to use and why.
- Solve simple measure and money problems involving fractions and decimals to two decimal places.
- Find 1000 less than a given number.
- Count backwards through zero, including negative numbers.
- Recognise place value of each digit in a 4-digit number, round any number to the nearest 10 , 100 or 1000 and use this knowledge to solve subtraction problems.
- Solve number and practical problems that involve the above, with increasingly large positive numbers.

Year 5 subtract with at least 4-digit numbers including money, measures, decimals.

Compact column subtraction
(with 'exchanging').

Subtracting with larger integers.


Subtract with decimal values, including mixtures of integers and decimals, aligning the decimal point.


Add a 'zero' in any empty decimal places to aid understanding of what to subtract in that column (place holder).

Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, difference/how many between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit, inverse, tenths, hundredths, decimal point, decimal.

## Key skills for subtraction at Y 5 :

- Subtract numbers mentally with increasingly large numbers.
- Use rounding and estimation to check answers to calculations and determine, in a range of contexts, levels of accuracy.
- Solve addition and subtraction multi-step problems in context, deciding which operations and methods to use and why.
- Read, write, order and compare numbers to at least 1 million and determine the value of each digit.
- Count forwards or backwards in steps of powers of 10 for any given number up to 1 million.
- Interpret negative numbers in context, counting forwards and backwards with positive and negative integers through 0.
- Round any number up to 1 million to the nearest 10, 100, 1000, 10000 and 100000.



## Key vocabulary: equal to, take, take away, less, minus, subtract, leaves, difference/how many

 between, how many more, how many fewer/less than, most, least, count back, how many left, how much less is_? difference, count on, strategy, partition, tens, units exchange, decrease, hundreds, value, digit, inverse, tenths, hundredths, decimal point, decimal.
## Key skills for subtraction at Y6:

- Solve addition and subtraction multi-step problems in context, deciding which operations and methods to use and why.
- Read, write, order and compare numbers up to 10 million and determine the value of each digit.
- Round any whole number to a required degree of accuracy.
- Use negative numbers in context, and calculate intervals across zero.
- Children need to utilise and consider a range of mental subtraction strategies, jottings and written methods before choosing how to calculate.


## Reception Begin to count in steps of 2, 5 and 10 and double numbers to 20 using concrete objects and pictures.



- Give children experience of counting equal group of objects in $2 s, 5 s$ and $10 s$.
- Children to work with real life contexts and use practical equipment to count in steps of 2,5 and 10.
- Children to sing songs, role play and use concrete objects.
- Children begin to record in the context of play or practical activities.


## Key vocabulary: count in steps of...

Key skills for multiplication in Reception:

- Count in steps of 2,5 and 10 practically, pictorially and through the use of play based learning.
- To double numbers up to 10 .



## Key vocabulary: groups of, lots of, times, array, altogether, multiply, count.

## Key skills for multiplication at Y 1 :

- Count in multiples of 2,5 and 10.
- Solve one-step problems involving multiplication, by calculating the answer using concrete objects, pictorial representations, repeated addition and arrays with the support of the teacher.
- Make connections between arrays, number patterns, and counting in twos, fives and tens.
- Begin to understand doubling using concrete objects and pictorial representations.

Year 2 Multiply using arrays and repeated addition (using at ..us. $2 \mathrm{~s}, 5 \mathrm{~s}$ and 10 s ).

## Use repeated addition on a number line:

- Starting from zero, make equal jumps along a number line to work out multiplication facts and write multiplication statements using $x$ and $=$ signs.



## Use arrays:



$$
3 \times 5=15
$$

Use arrays to help teach children to understand the commutative law of multiplication, and give examples such as $3 \times$ $\qquad$ $=6$.

Use practical apparatus:

```
5\times3=5+5+5
O
```


## Use mental recall:

- Children should begin to recall multiplication facts for 2, 5 and 10 times tables through practice in counting and understanding of the operation.


## Year 2 Multiplication (continued)

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times...

## Key skills for multiplication at Y 2 :

- Count in steps of 2,3 and 5 from zero, and in 10 s from any number.
- Recall and use multiplication facts for 2,5 and 10, including recognising odds and evens.
- Write and calculate number statements using the $\times$ and $=$ signs.
- Show that multiplication can be done in any order (commutative).
- Solve a range of problems involving multiplication, using concrete objects, arrays, repeated addition, mental methods, and multiplication facts.
- Pupils use a variety of language to discuss and describe multiplication.


## Year 3 Multiply 2-digits by a single digit number.

Introduce the grid method for multiplying 2-digit by singledigits:

Link the layout of the grid to an array initially:
Eg. $\quad 23 \times 8=184$

| $X$ | 20 | 3 |
| :---: | :---: | :---: |
| 8 | 160 | 24 |

$160+24=184$


Introduce the grid method with children physically making an array to represent the calculation (e.g. make 8 lots of 23 with 10 s and 1 s place value counters), then translate this to grid method format.

To do this, children must be able to:

- Partition numbers into tens and units.
- Multiply multiples of ten by a single digit (e.g. $20 \times 4$ ) using their knowledge of multiplication facts and place value.
- Recall and work out multiplication facts in the 2, 3, 4, 5, 8 and 10 times tables.
- Work out multiplication facts not known by repeated addition or other taught mental strategies (e.g. by commutative law, working out near multiples and adjusting, using doubling etc.) Strategies to support this are repeated addition using a number line, bead bars and arrays:



## Year 3 Multiplication (continued)

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, times, _times as big as, once, twice, three times..., partition, grid method, multiple, product, tens, units, value.

## Key skills for multiplication:

- Recall and use multiplication facts for the 2, 3, 4, 5, 8 and 10 multiplication tables, and multiply multiples of 10.
- Write and calculate number statements using the multiplication tables they know, including 2-digit $\times$ single-digit, drawing upon mental methods, and progressing to reliable written methods.
- Solve multiplication problems, including missing number problems.
- Develop mental strategies using commutativity e.g. $(4 \times 12) \times 5=(4 \times 5) \times 12=20 \times$ $12=240$.
- Solve simple problems in contexts, deciding which operations and methods to use.
- Develop efficient mental methods to solve a range of problems e.g. using commutativity (see above) and for missing number problems

$$
\text { _ } \times 5=20 \quad 3 x_{-}=18
$$

Year 4 Multiply 2 and 3 -digits by a single digit, using all multiplication tables up to $12 \times 12$.

## Developing the grid method:



Children should be able to:

- Approximate before they calculate, and make this a regular part of their calculating, going back to the approximation to check their answer. e.g.
" $346 \times 9$ is approximately $350 \times 10=3500$ "
Record an approximation to check the final answer against.
- Multiply multiples of ten and one hundred by a single-digit, using their multiplication table knowledge.
- Recall all times tables up to $12 \times 12$.


## Year 4 Multiplication (continued)

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, array, column, row, commutative, groups of, sets of, lots of, equal groups, times, multiply, times as big as, once, twice, three times... partition, grid method, total, multiple, product, sets of, inverse.

Key skills for multiplication at Y4:

- Count in multiples of 6,7,9,25 and 1000.
- Recall multiplication facts for all multiplication tables up to $12 \times 12$.
- Recognise place value of digits in up to 4-digit numbers and use this to solve multiplications.
- Use place value, known facts and derived facts to multiply mentally, e.g. multiply by $1,10,100$, by 0 , or to multiply 3 numbers.
- Use commutativity and other strategies mentally $3 \times 6=6 \times 3,2 \times 6 \times 5=10 \times 6$, $39 \times 7=(30 \times 7)+(9 \times 7)$.
- Solve problems with increasingly complex multiplication in a range of contexts.


## Year 5 Multiply up to 4-digits by 1 or 2 digits.

Introducing column multiplication:

- Introduce by comparing a grid method calculation to a short multiplication method, to see how the steps are related, but notice how there are less steps involved in the column method.
- Children need to be taught to approximate first, e.g. for $72 \times 38$, they will use rounding: $72 \times 38$ is approximately $70 \times 40=2800$, and use the approximation to check the reasonableness of their answer.


## Short multiplication for multiplying by a single digit:

| $x$ | 300 | 20 | 7 |
| :---: | :--- | :---: | :---: |
| 4 | 1200 | 80 | 28 |



Pupils could be asked to work out a given calculation using the grid, and then compare it to 'your' column method. What are the similarities and differences? Unpick the steps and show how it reduces the steps.

Introduce long multiplication for multiplying by 2 digits:


## Year 5 Multiplication (continued)

Key vocabulary groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative, sets of, equal groups, _times as big as, once, twice, three times..., partition, grid method, total, multiple, product, inverse, square, factor, integer, decimal, short/long multiplication, 'carry'.

Key skills for multiplication at Y 5 :

- Identify multiples and factors, using knowledge of multiplication tables to $12 \times 12$.
- Solve problems where larger numbers are decomposed into their factors.
- Multiply and divide integers and decimals by 10, 100 and 1000.
- Recognise and use square and cube numbers and their notation.
- Solve problems involving combinations of operations, choosing and using calculations and methods appropriately.

Year 6 Short and long multiplication as in Y5, and multiply decimals with up to 2 decimal places by a single digit.


- Use rounding and place value to make approximations before calculating and use these to check answers.
- Use short multiplication (see V 5 ) to multiply numbers with more than 4digits by a single digit.
- Multiply money and measures and multiply decimals with up to 2 decimal places by a single digit.
- Use long multiplication (see Y 5 ) to multiply numbers with at least 4 digits by a 2-digit number.


## Year 6 Multiplication (continued)

Key vocabulary: groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, array, column, row, commutative, sets of, equal groups, times as big as, once, twice, three times... partition, grid method, total, multiple, product, inverse, square, factor, integer, decimal, short / long multiplication, 'carry', tenths, hundredths, decimal.

## Key skills for multiplication at Y6:

- Recall multiplication facts for all times tables up to $12 \times 12$ (as Y4 and Y5).
- Multiply multi-digit numbers, up to 4-digit x 2-digit using long multiplication.
- Perform mental calculations with mixed operations and large numbers.
- Solve multi-step problems in a range of contexts, choosing appropriate combinations of operations and methods.
- Estimate answers using rounding and approximation and determine levels of accuracy.
- Round any integer to a required degree of accuracy.


## Reception Practically share small quantities between 2

 people.Using objects and pictorial representations to share a small set of objects into equal groups.

Can you share 4 sweets between these two children?


- Use lots of practical apparatus and pictorial representations.
- To share objects in a range of familiar contexts and through the use of roleplay.

Key Vocabulary: share, one each, two each..., lots of.
Key number skills needed for division in Reception:

- To count in steps of 2,5 and 10.
- To double and halve numbers up to 20.


## Year 1 Group and share small quantities

Using objects, diagrams and pictorial representations to solve problems involving both grouping and sharing.

How many groups of 4 can be made with 12 stars? $=3$

## Grouping

## Sharing



4


12 shared between 3 is 4

Example division problem in a familiar context:

There are 6 pupils on this table and there are 18 pieces of fruit to share between us. If we share them equally, how many will we each get?

Can they work it out and give a division statement... ?
"18 shared between 6 people gives you 3 each."

- Use lots of practical apparatus and pictorial representations.
- Be taught to understand the difference between 'grouping' objects (How many groups of 2 can you make?) and 'sharing' (Share these sweets between 2 people)
- Be able to count in multiples of 2,5 and 10 .
- Find half of a group of objects by sharing into 2 equal groups.


## Year 1 Division (continued)

Key Vocabulary: share, share equally, one each, two each..., group, groups of, lots of.

Key number skills needed for division at Y 1 :

- Solve one-step problems involving division, by calculating the answer using concrete objects and pictorial representations with the support of the teacher.
- Through grouping and sharing small quantities, pupils begin to understand, division, and finding simple fractions of objects, numbers and quantities.
- They make connections between number patterns and counting in twos, fives and tens.

Year 2 Group and share, using the $\div$ and $=$ sign

Use objects, arrays, diagrams and pictorial representations, and grouping on a number line.

Arrays :

$12 \div 3=4$

This represents $12 \div 3$, posed as how many groups of 3 are in 12?

Pupils should also show that the same array can represent $12 \div 4=3$ if grouped horizontally.

## Know and understand sharing and grouping:

6 sweets shared between 2 people, how many do they each get?


Children should be taught to recognise whether problems require sharing or grouping.

## Grouping using a number line:

Group from zero in equal jumps of the divisor to find out "how many groups of _in _ ?". Pupils could and using a bead string or practical apparatus to work out problems like "A CD costs $£ 3$. How many CDs can I buy with $£ 12$ ?" This is an important method to develop understanding of division as grouping.

[^0]
## Year 2 Division (continued)

Key Vocabulary: share, share equally, one each, two each....
group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over.

Key number skills needed for division at Y 2 :

- Count in steps of 2,3 , and 5 from 0 .
- Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers.
- Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the $x, \div$ and $=$ symbols.
- Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.
- Solve problems involving division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

Year 3 Divide 2-digit numbers by a single digit (where there is a remainder in the final answer).


Grouping on a number line:

$$
13 \div 4=3 r 1
$$


rl
5
9
13


Once children are secure with division as grouping and demonstrate this using number lines, arrays etc. short division for larger 2-digit numbers should be introduced, initially with carefully selected examples requiring no calculating of remainders at all. Start by introducing the layout of short division by comparing it to an array.

Remind children of correct place value (that 96 is equal to 90 and 6) but in short division, pose:

- How many 3 " $\sin$ in $=3$, and record it above the 9 tens.
- How many 3 "'s in 6 ? $=2$, and record it above the 6 units


## Year 3 Division (continued)

## Short division:

Once children demonstrate a full understanding of remainders, and also the short division method taught, they can be taught how to use the method when remainders occur within the calculation and be taught to 'carry' the remainder onto the next digit.

If needed, children should use the number line to work out individual division facts that occur which they are not yet able to recall mentally.

Real life contexts need to be used routinely to help pupils gain a full understanding, the ability to recognise the place of division and how to apply it to problems.

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple.

Key number skills needed for division at Y3:

- Recall and use multiplication and division facts for the $2,3,4,5,8$ and 10 multiplication tables (through doubling, connect the 2, 4 and 8 s ).
- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know - using mental methods and progressing to formal written methods.
- Solve problems in a range of contexts including missing number problems involving multiplication and division.
- Pupils develop efficient mental methods, for example, using multiplication and division facts (e.g. using $3 \times 2=6,6 \div 3=2$ and $2=6 \div 3$ ) to derive related facts ( 30 $\times 2=60$, so $60 \div 3=20$ and $20=60 \div 3$ ).
- Pupils develop reliable written methods for division, starting with calculations of 2digit numbers divided by 1-digit numbers and progressing to the formal written method of short division.


## Year 4 Divide up to 3-digit numbers by a single digit

(without remainders initially).

## Continue to develop short division:



STEP 1: Pupils must be secure with the process of short division for dividing 2 -digit numbers by a single digit (those that do not result in a final remainder - see steps in Y 3 ), but must understand how to calculate remainders, using this to 'carry' remainders within the calculation process (see example).

STEP 2: Pupils move onto dividing numbers with up to 3digits by a single digit, however problems and calculations provided should not result in a final answer with remainder at this stage. Children who exceed this expectation may progress to Y 5 level.


When the answer for the first column is zero ( $1 \div 5$, in this example), children could initially write a zero above to acknowledge its place, and must always 'carry' the number ( 1 in this example) over to the next digit as a remainder (to become $18 \div 5$ ).


Real life contexts need to be used routinely to help pupils gain a full understanding, and the ability to recognise the place of division and how to apply it to problems.

## Year 4 Division (continued)

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, divisible by, factor.

Key number skills needed for division at Y 4 :

- Recall multiplication and division facts for all numbers up to $12 \times 12$.
- Use place value, known and derived facts to divide mentally, including dividing by 10,100 and 1.
- Pupils practise to become fluent in the formal written method of short division with exact answers when dividing by a one-digit number.
- Pupils practise mental methods and extend this to three-digit numbers to derive facts, for example $200 \times 3=600$ so $600 \div 3=200$.
- Pupils solve two-step problems in contexts, choosing the appropriate operation, working with increasingly harder numbers. This should include correspondence questions such as three cakes shared equally between 10 children.

Year 5 Divide up to 4 digits by a single digit, including
 those with remainders.

Short division, including remainder answers:


Short division with remainders: Now that pupils are introduced to examples that give rise to remainder answers, division needs to have a real life problem solving context, where pupils consider the meaning of the remainder and how to express it i.e. as a fraction, a decimal, or as a rounded number or value, depending upon the context of the problem.

Include money and measure contexts.

See Y6 for how to continue the short division to give a decimal answer for children who are confident.

## If children are confident and accurate:

- Introduce long division for pupils who are ready to divide any number by a 2digit number (e.g. $2678 \div 19$ ). This is a Year 6 expectation.


## Year 5 Division (continued)

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, divisible by, factor, inverse, quotient, prime number, prime factors, composite number (non-prime).

Key number skills needed for division at Y 5 :

- Recall multiplication and division facts for all numbers up to $12 \times 12$ (as in Y4).
- Divide numbers mentally, drawing upon known facts.
- Identify multiples and factors, including finding all factor pairs of a number, and common factors of two number.
- Solve problems involving division where larger numbers are decomposed into their factors.
- Divide whole numbers and those involving decimals by 10,100 and 1000.
- Use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers.
- Work out whether a number up to 100 is prime, and recall prime numbers to 19 .
- Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.
- Use multiplication and division as inverses.
- Interpret non-integer answers to division by expressing results in different ways according to the context, including with remainders, as fractions, as decimals or by rounding (e.g. $98 \div 4=24 \mathrm{r} 2=24 \frac{1}{2}=24.5 \approx 25$ ).
- Solve problems involving combinations of all four operations, including understanding of the equals sign, and including division for scaling by different fractions and problems involving simple rates.

Year 6 Divide at least 4 digits by both single-digit and
2-digit numbers (including decimal numbers and quantities).
Short division, for dividing by a single digit: e.g. $6497 \div 8$


Short division with remainders: Pupils should continue to use this method, but with numbers to at least 4 digits, and understand how to express remainders as fractions, decimals, whole number remainders, or rounded numbers. Real life problem solving contexts need to be the starting point, where pupils have to consider the most appropriate way to express the remainder.

Calculating a decimal remainder: In this example, rather than expressing the remainder as $\mathbf{r 1}$, a decimal point is added after the units because there is still a remainder, and the one remainder is carried onto zeros after the decimal point (to show there was no decimal value in the original number). Keep dividing to an appropriate degree of accuracy for the problem being solved.

Introduce long division by chunking for dividing by 2 digits.

|  | $2$ | Find out "How 972?" by sub 36, until zero until there is <br> Teach pupils list' first at help them de use, e.g.: 'Useful' list: | $y 36$ are in ing 'chunks' of ached (or mainder). <br> ite a 'useful de that will what chunks to $\begin{aligned} & 1 x=36 \\ & 10 x=360 \\ & 100 x=3600 \end{aligned}$ | Where remainders occur, pupils should express them as fractions, decimals or use rounding, depending upon the problem. |
| :---: | :---: | :---: | :---: | :---: |

## Year 6 Division (continued)

Continuation of long division by chunking for dividing by 2 digits (Y6)

Introduce the method in a simple way by limiting the choice of chunks to "Can we use 10 lots? Can use 100 lots?" As children become confident with the process, encourage more efficient chunks to get to the answer more quickly (e.g. 20x, $5 x$ ), and expand on their 'useful' lists.

Key Vocabulary: share, share equally, one each, two each..., group, equal groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, inverse, short division, 'carry', remainder, multiple, divisible by, factor, inverse, quotient, prime number, prime factors, composite number (non-prime), common factor.

Key number skills needed for division at Y6:

- Recall and use multiplication and division facts for all numbers to $12 \times 12$ for more complex calculations
- Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context. Use short division where appropriate.
- Perform mental calculations, including with mixed operations and large numbers.
- Identify common factors, common multiples and prime numbers.
- Solve problems involving all 4 operations.
- Use estimation to check answers to calculations and determine accuracy, in the context of a problem.
- Use written division methods in cases where the answer has up to two decimal places.
- Solve problems which require answers to be rounded to specified degrees of accuracy.

This policy was approved by Governors on Wednesday $1^{\text {st }}$ March 2017 and will be reviewed in February 2018.

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[^0]:    Pose $12 \div 3$ as 'How many groups of 3 are in 12?"

